

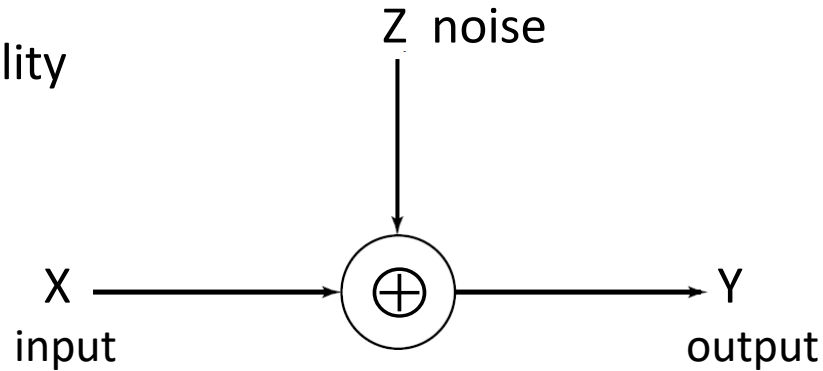
# ELEC 515

## Information Theory

### Continuous Channel Capacity

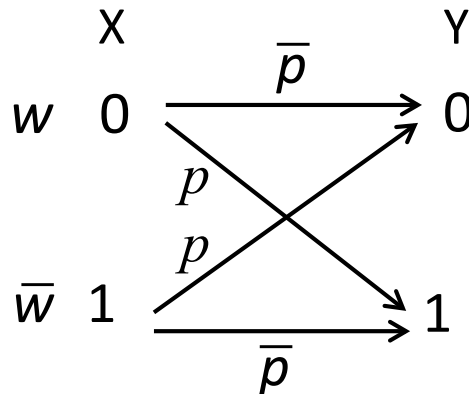
# BSC Channel Capacity

crossover probability  
 $p = \Pr(z = 1)$



$$\Pr(x = 0) = w$$

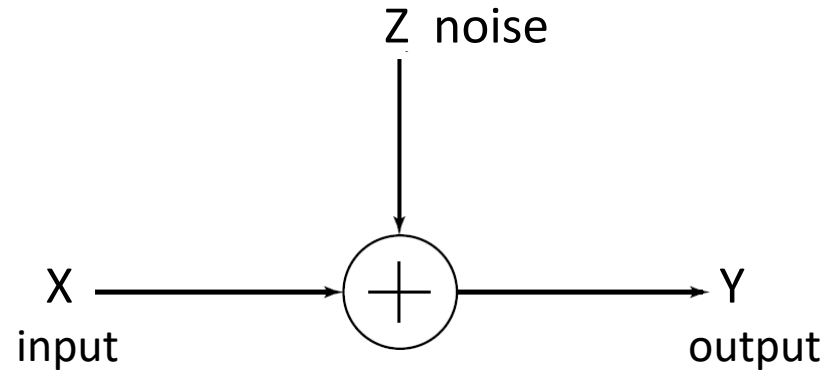
$$\Pr(x = 1) = 1 - w = \bar{w}$$



$$w = \bar{w} = \frac{1}{2}$$

$$C = 1 - h(p)$$

# AWGN Channel Capacity



$$f_z(z) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp\left[-\frac{(z-\mu)^2}{2\sigma^2}\right]$$

# Differential Entropy

- Continuous random variable  $X$  with pdf  $f(x)$
- The differential entropy of  $X$  is defined as

$$H(X) = -\int_S f(x) \log f(x) dx$$

where  $S$  is the support set of  $X$  (values of  $x$  for which  $f(x) > 0$ )

# AWGN Channel Capacity

$$C = W \log_2 \left( 1 + \frac{P}{N_0 W} \right)$$

$$E = PT \rightarrow P = E_b R_b$$

$$C = W \log_2 \left( 1 + \frac{E_b R_b}{N_0 W} \right)$$

Let  $R_b = C$

$$\frac{C}{W} = \log_2 \left( 1 + \frac{E_b}{N_0} \frac{C}{W} \right)$$

$$\frac{E_b}{N_0} = \frac{2^{C/W} - 1}{C/W}$$

# Bandwidth Efficiency versus SNR

