

From Manual Drafting to CAD

- Electronic drafting using a Computer-Aided Drafting (CAD) system
- Computer graphics and geometric modeling
- Design modeling using an advanced CAD/CAE/CAM system
- Finite element analysis
- Engineering optimization
- Virtual (Soft) prototyping

Questions

- What are the basic CAD techniques?
 - Geometric representation and transformation
 - Solid and surface modeling
 - Parametric modeling and parameter optimization
 - Pre- and post- processors for Finite Element Analysis
 - Design and Mfg. database management
- What are the differences between a conventional 2D electronic drafting package and a full-scale CAD/CAE/CAM system?
(Computer-Aided Design, Engineering and Manufacturing)
- What do we need to know to be a better user of the CAD system?
 - The basic CAD techniques
 - The capabilities and limitations of various CAD systems

Development of CAD

- **In 1960's**
 - mechanism design satisfying several geometric constraints
 - design parameter optimization
 - simple 2-D graphics
- **In 1970's**
 - wireframe modeling
 - free-form surface modeling – *mainframe computers*
- **Late 1970's**
 - solid modeling
- **Early 1980's**
 - CAD/CAM integration
 - mechanical feature recognition from a CAD database

Development of CAD

- **Middle 1980's**

- feature-based CAD system – *mini and micro computers,*
- parametric design – *PC's & Turnkey systems*
(Pro/ENGINEER Products)

- **Late 1980's**

- design for manufacturing
- design for automated assembly

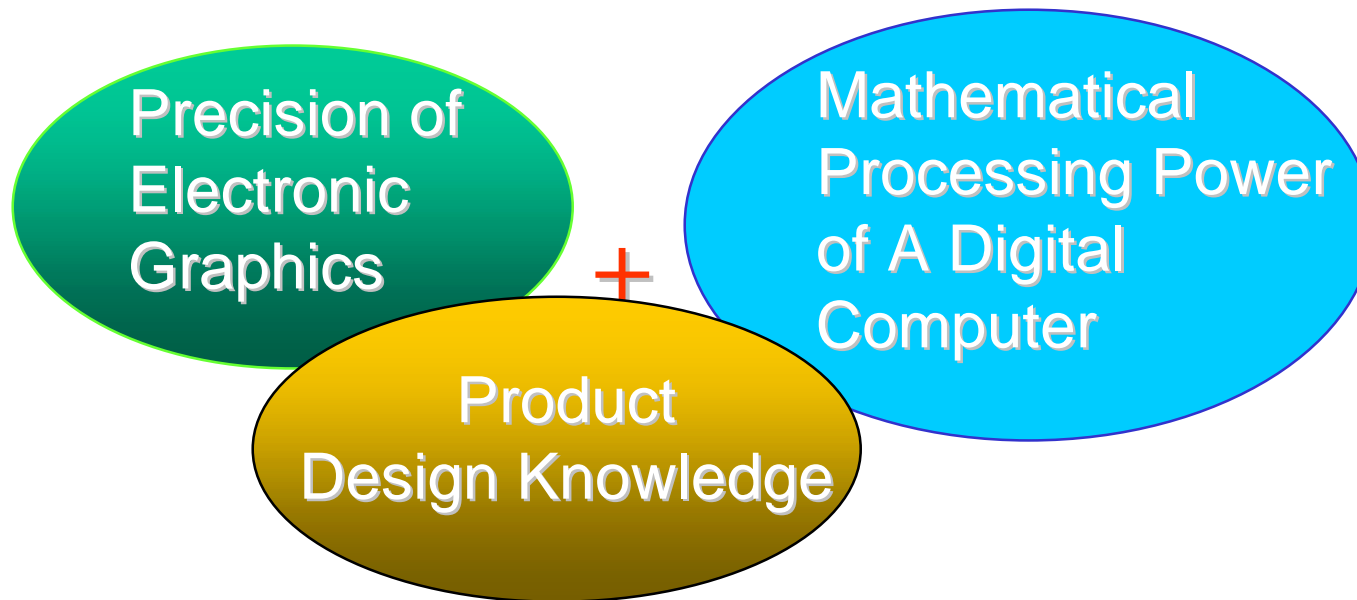
- **1990's**

- concurrent engineering design
- integrated design, analysis and optimization
- virtual-prototyping – *workstations and high-end PCs*

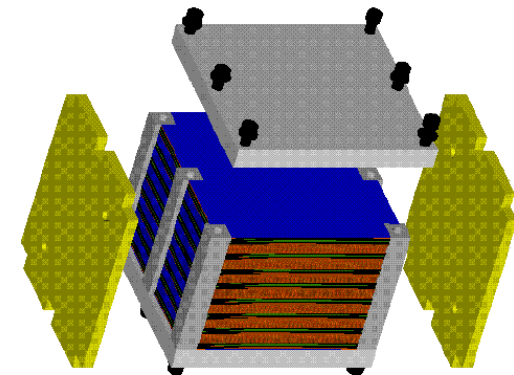
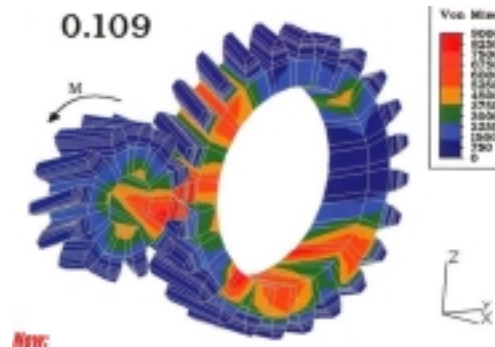
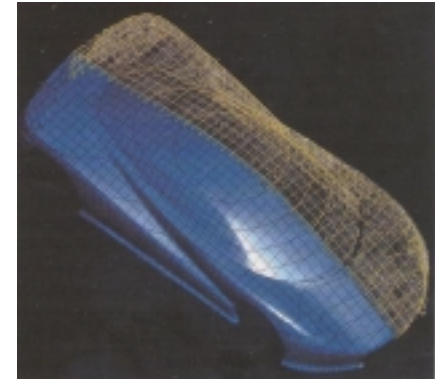
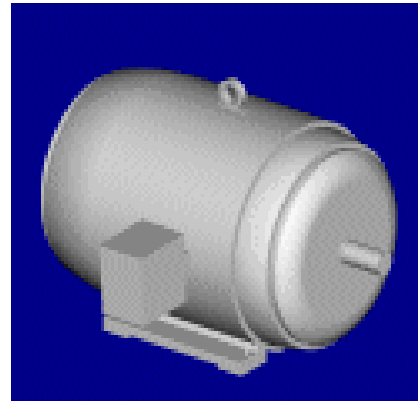
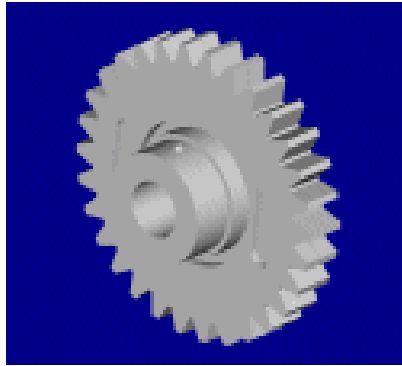
- **2000's**

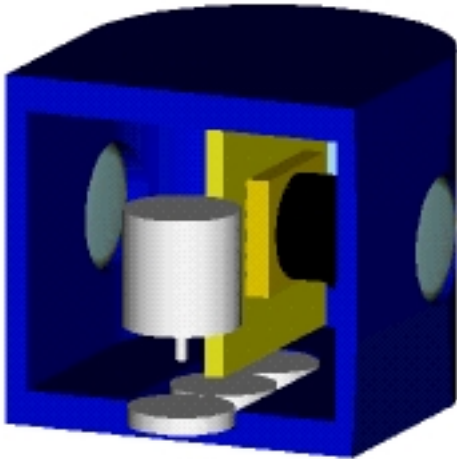
- robust concurrent design optimization
- virtual engineering & enterprise

Unique Characteristics of A CAD System



How are these models generated?



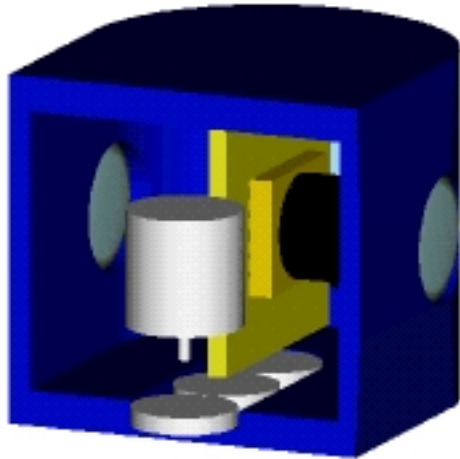


How is Geometry represented in a CAD system?

- Wireframe Model (low-level entities)
Points and Lines
- Solid Model (middle to high-level entities)
Points, Primitives and Boolean Operations
- Surface Model (middle-level entities)
Points, Boundary and Control Curves; Surface Patches

Representation of Low-level Geometry Entities:

- Points: A 2D point – $[x \ y]$; and A 3D point – $[x \ y \ z]$
A vector representation of a 3D point: $\mathbf{p} = x\mathbf{i} + y\mathbf{j} + z\mathbf{k}$
- Lines: two points
- Planes: a collection of boundary lines
- Components: a collection of boundary planes

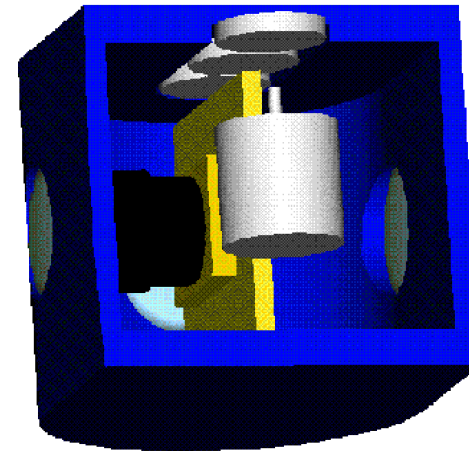


Why geometry transformation?

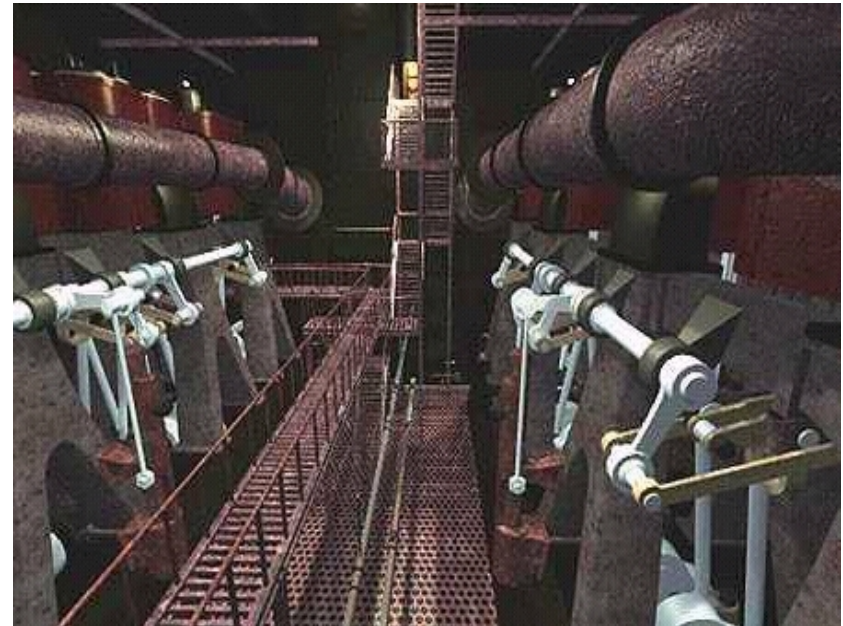
- Better understanding of the design
- Communication with customers
- Generating various outputs

Common transformations:

- Translation
- Rotation
- Scaling



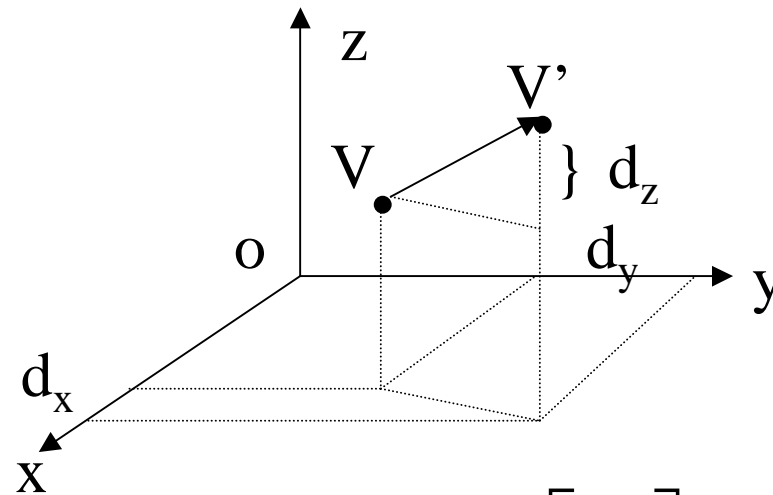
Applications of geometry transformation?



3-D Transformation

Translation

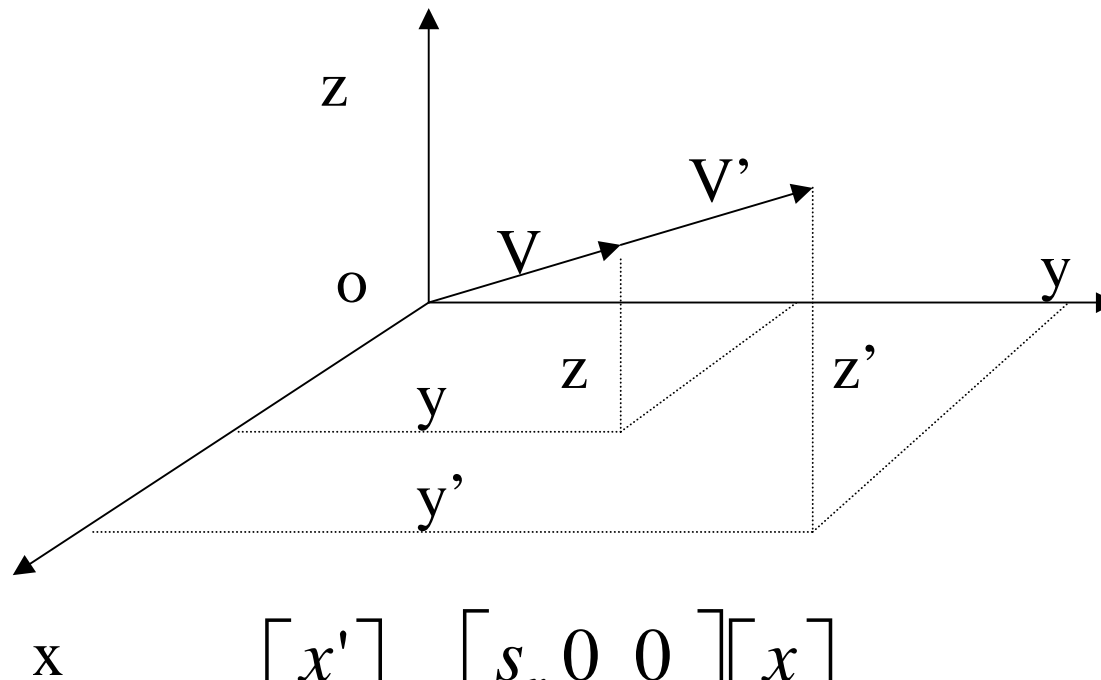
Translate point $V(x, y, z)$ by (dx, dy, dz) to point $V'(x', y', z')$



$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} x \\ y \\ z \end{bmatrix} + \begin{bmatrix} d_x \\ d_y \\ d_z \end{bmatrix}$$

3-D Transformation

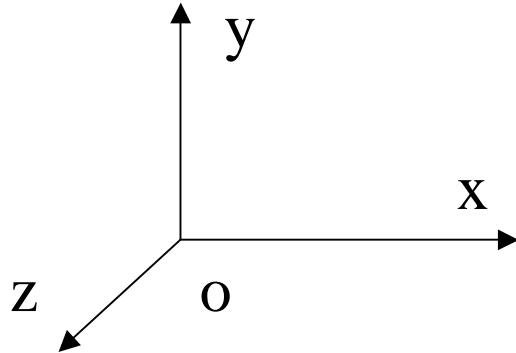
Scaling



$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} s_x & 0 & 0 \\ 0 & s_y & 0 \\ 0 & 0 & s_z \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

3-D Transformation

Rotation

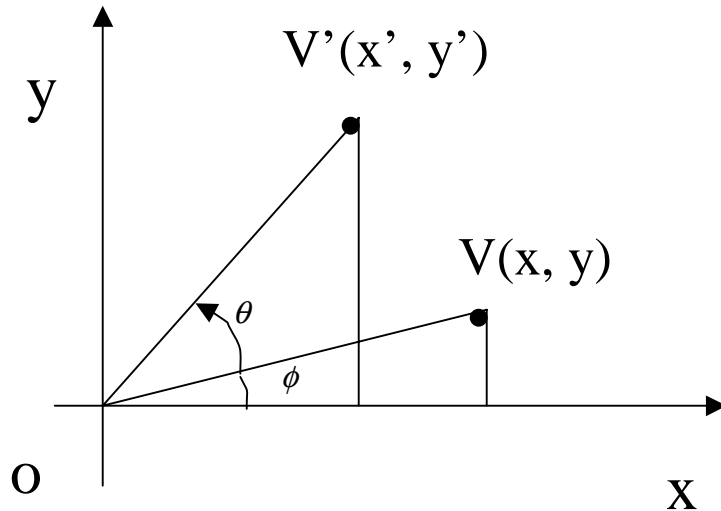


About z

$$z' = z$$

$$x' = x \cos \theta - y \sin \theta$$

$$y' = x \sin \theta + y \cos \theta$$



$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

3-D Transformation

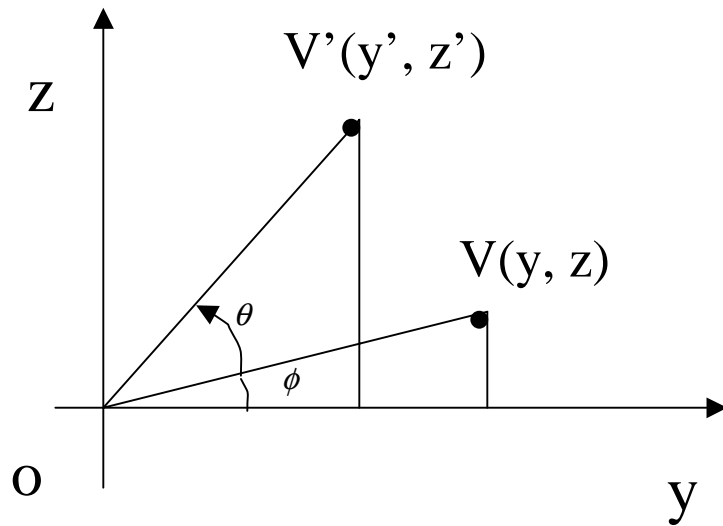
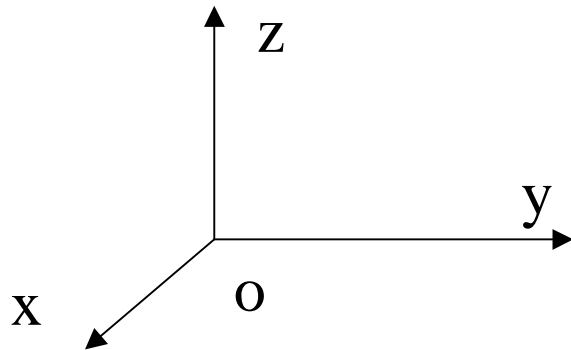
Rotation

About x

$$x' = x$$

$$y' = y \cos \theta - z \sin \theta$$

$$z' = y \sin \theta + z \cos \theta$$



$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta \\ 0 & \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

3-D Transformation

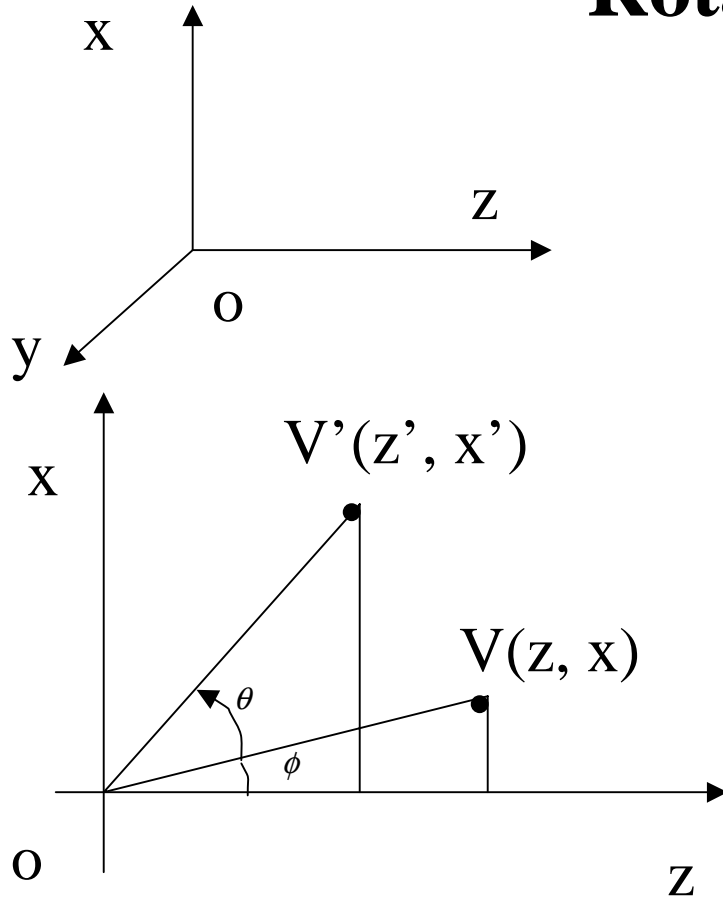
Rotation

About y

$$y' = y$$

$$x' = z \sin \theta + x \cos \theta$$

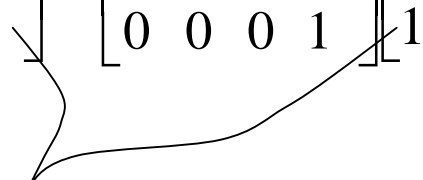
$$z' = z \cos \theta - x \sin \theta$$



$$\begin{bmatrix} x' \\ y' \\ z' \end{bmatrix} = \begin{bmatrix} \cos \theta & 0 & \sin \theta \\ 0 & 1 & 0 \\ -\sin \theta & 0 & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

Homogeneous Representation

The representation is introduced to express all geometric transformations in the form of matrix multiplication for the convenience of manipulation.

$$\begin{bmatrix} x' \\ y' \\ z' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & d_x \\ 0 & 1 & 0 & d_y \\ 0 & 0 & 1 & d_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix}$$


Dummy (n+1)th coordinate to facilitate multiplication

Homogeneous Representations

Scaling

$$[H] = \begin{bmatrix} s_x & 0 & 0 & 0 \\ 0 & s_y & 0 & 0 \\ 0 & 0 & s_z & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Rotation

$$[H_y] = \begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Composition of Transformation

$$V' = [H_n][H_{n-1}] \cdots [H_1]V$$