# Localization in Wireless Sensor Network ELEC 619B Presentation

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# Motivation and Problem Statement

Motivation: Increasing availability of low-cost, portable, smart sensors that can be deployed in large numbers in a wireless sensor network (WSN).

Applications: Environmental monitoring, inventory management, intrusion detection, and traffic monitoring  $\rightarrow$  "sensing data without knowing the sensor location is meaningless."

#### Localization Problem [Boukerche'07]

Given a multihop network G = (V, E), and a set of beacon nodes  $\mathcal{B}$  and their positions  $(x_b, y_b)$ , for all  $b \in \mathcal{B}$ , we want to find the position  $(x_u, y_u)$  of as many unknown nodes  $u \in \mathcal{U}$  as possible.

# Components of a Localization System [Boukerche'07]



Distance/angle estimation: Estimating position related parameters between two nodes.

Position computation: Computing a node's position based on available information and anchor nodes positions.

Localization algorithm: Manipulating available information in order to localize other nodes in a WSN.

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# Distance/Angle Measurement Techniques [Boukerche'07]



- a) Received signal strength (RSS):  $\hat{d}_{ij} = d_0 (P_0/P_{ij})^{1/n_p}$  [Patwari'03], low cost but very susceptible to noise.
- b) Time-of-arrival (ToA):  $\hat{d} = c(t_2 t_1)$ , accurate but requires synchronization.
- c) Time-difference-of-arrival (TDoA):  $\hat{d} = (c s_s)(t_2 t_1)$  or  $\hat{d} = \hat{d}_i \hat{d}_0$ , no synchronization necessary but costly.
- d) Angle-of-arrival (AoA):  $\phi = \frac{2\pi d \cos \theta}{\lambda}$ , costly and requires extensive signal processing.



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## Multilateration/Triangulation/NLS Estimator



a) - c) Multilateration linear least-squares (LLS): Subtract  $\hat{d}_i^2 = (x - x_i)^2 + (y - y_i)^2$ , from *r*-th measurement to obtain  $2(x_i - x_r)x + 2(y_i - y_r)y = \hat{d}_r^2 - \hat{d}_i^2 - (x_r^2 + y_r^2) + (x_i^2 + y_i^2)$ , for  $i = 1, \dots, N - 1$  [Gezici'08a]. e), f) Triangulation LLS: We have  $x = x_i + \hat{d}_i \cos \hat{\alpha}_i$  and  $y = y_i + \hat{d}_i \sin \hat{\alpha}_i$ , for  $i = 1, \dots, N$  [Sayed'05].

• Non-linear LS (NLS) & maximum likelihood estimator (MLE):  $\hat{\theta} = \arg \min_{\tilde{\theta}} \sum_{i=1}^{N} \frac{(z_i - f_i(x,y))^2}{\sigma_i^2}$ , requires good initialization [Mao'07, Gezici'08].



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# Dv-Hop Ad Hoc Positioning System [Niculescu'01]



- a) Beacon nodes broadcast their position information;
- b) Beacon nodes compute the average one hop size from position information of other Beacons;
- c) Unknown nodes convert number of hops from a beacon to distance.

# Recursive Position Estimation (RPE) [Albowicz'01]



- a) An unknown node determines its reference nodes;
- b) The unknown node estimates its distance to these references;
- c) The unknown node computes its position using multilateration;
- d) Now, the unknown node becomes a settled node and assists other nodes in position estimation.

## Traditional vs. Cooperative Localization [Patwari'05]



Centralized: MLE [Patwari'03], Convex Optimization, e.g., SDP [Doherty'01, Biswas'06], MDS [Cheung'05, Shang'03] etc. Distributed: APS [Niculescu'01], RPE [Albowicz'01, Savvides'01], MDS [Ji'04], dwMDS [Costa'06], SOCP [Srirangarajan'08], etc.

# Performance of Cooperative Localization [Patwari'05]



Left:  $K^2$  sensors with 4 anchors (×) and  $K^2 - 4$  unknown nodes (•) in a  $L \times L$  m<sup>2</sup> area. Right:  $\sigma_{dB}/n_p = 1.7$ ,  $\sigma_T = 6.3$  ns,  $\sigma_{\alpha} = 5$ , r is radius of connectivity in a  $20 \times 20$  m<sup>2</sup> area.

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# Thank You!

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