

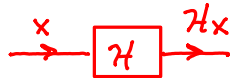
**Example 2.6.** For a system operator  $\mathcal{H}$ , a function  $x$ ,<sup>a real variable  $t$ ,</sup> and a real constant  $t_0$ , the expression  $\mathcal{H}x(t-t_0)$  denotes the result obtained by taking the function  $y$  produced as the output of the system  $\mathcal{H}$  when the input is the function  $x$  and then evaluating  $y$  at  $t-t_0$ . ■

$\mathcal{H}$  is a system.



$\mathcal{H}x$  is the output of the system  $\mathcal{H}$  when the input is  $x$ .

$\underbrace{\mathcal{H}x}_{\text{function}} \quad \underbrace{x}_{\text{function}}$



Since  $\mathcal{H}x$  is a function, we can evaluate it at some point such as  $t-t_0$ .

$\mathcal{H}x(t-t_0)$

$\underbrace{\mathcal{H}x}_{\text{function}} \quad \underbrace{(t-t_0)}_{\substack{\text{number} \\ \text{point at} \\ \text{which} \\ \text{function is} \\ \text{evaluated}}}$