Analysis of a Class-B Microwave-Photonic Link Using Optical Frequency Modulation

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Abstract—A class-B microwave-photonic link using optical frequency modulation (FM) and fiber-Bragg gratings (FBGs) is analyzed and results verified with measurements. Input voltage is converted linearly to FM, and this FM is converted by each FBG to intensity modulation. For small FM index β , the signal increases as β^3 , becoming linear in β with a frequency offset or carrier leakage, and third-order distortion resulting from the detection process is shown to be worse than that obtained using a Mach–Zehnder intensity modulator at the same modulation index. For large $\beta(> 10)$, third-order distortion approaches zero and ideal class-B operation is predicted, and the only shot noise and relative intensity noise (RIN) added is that which arises from the detected signal power.

Index Terms—Class B, microwave-photonic link (MPL), optical frequency modulation (FM), optical link, radio over fiber, spur-free dynamic range.

I. INTRODUCTION

M ICROWAVE-PHOTONIC links (MPLs) play an important role in many applications including video distribution networks, radio-over-fiber, and radar systems. In each application, noise and distortion limit the spur-free dynamic range (SFDR) of signals that can be transmitted [1]. Increasing the dynamic range requires improving the linearity of the RF-tooptical converter, which increases the high-power limit to the SFDR, and reducing noise (intensity, shot, and receiver noise), which reduces the minimum detectable signal.

For traditional links using optical intensity modulation (IM) and direct detection, the high-power limit to the SFDR is limited by the linearity of the input voltage-output intensity transfer function of the modulated optical source. For low-frequency (<1 GHz) applications (e.g., hybrid fiber-coax cable television networks), direct modulation benefits from the intrinsic linearity of a laser current-output intensity response [2]. At higher frequencies, where carrier dynamics from direct modulation create undesirable resonance distortion, external modulation is used. Most existing high-performance links use Mach–Zehnder (MZ) modulators [3]. Although the sinusoidal MZ voltage-transmission transfer function introduces undesirable third-order distortion, the predictability of the response is well suited for electronic predistortion [4]. Electroabsorption modulators (EAMs) offer small size and low power [5], and may provide high linearity under limited operating conditions.

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Digital Object Identifier 10.1109/JLT.2008.927217

Even for a perfectly linear IM response, the high-end of the SFDR is limited by clipping, when the input voltage exceeds the maximum available optical power. This has been studied for cable signals [6] and more recently for MPLs [7], revealing that existing links fall far short of fundamental limits for linearity. Hence, effort continues to define alternative methods for providing high end-to-end system linearity.

Popular recent approaches include the use of FM or phase modulation (PM) with various forms of frequency or phase detectors. An interferometer can be used to detect PM, which may have several practical advantages [8], but otherwise preserves the sinusoidal transfer function of a MZ modulator. PM/FM can be detected using specially-fabricated FBGs [9], where the performance becomes defined by the fabrication of the gratings. Finally, PM can be detected using an optical phase-locked loop (OPPL) [10]. Under conditions of high loop gain, high linearity is achievable as the OPPL tracks the PM on the received optical signal. Loop stability is a challenge for high gain. So collectively, these approaches struggle to extend the SFDR at the high input signal limit by reducing distortion.

At the low input signal limit, noise reduction can also lead to large improvements in SFDR. Shot noise and relative intensity noise (RIN) powers scale linearly and quadratically in received optical power, respectively. Since for typical linear operating conditions much of the received optical signal power resides in the optical carrier, carrier suppression becomes an important objective. Examples of approaches explored to suppress the carrier include low-biasing an MZ [11], which reduces the response of the signal, and filtering the optical carrier [12], which adds distortion. Also, the use of PM/FM and FBGs can provide good linearity at low bias [9].

To maximize SFDR, it is essential to address both the high and low input power limits to the SFDR. This requires joint carrier suppression and linear modulation. An example of this was demonstrated [13], and extended into class AB [14]. This involves the use of complementary low-biased links to provide an effectively linear transfer function with zero average dc effective photocurrent. Ideally for class B, each link would half-wave rectify the input signal and the complete signal would be reconstructed at the output of a balanced photodetector. An ideal class B link has been analyzed [15], in which the only shot noise and RIN added is that which arises from the detected signal power, which can be well below receiver noise.

Unfortunately, while class B offers potentially high performance, implementation is challenged by the absence of an ideal linear threshold converter (ILTD). The ILTD must provide an output optical power of zero for input voltage >0 (or <0, for the

Manuscript received January 30, 2008; revised June 5, 2008. Current version published October 10, 2008. This work was supported by the NSERC.



Fig. 1. Class B optical link with PM/FM modulation, two FBGs, and balanced (differential) detection.

complementary ILTD), and linear response for voltages <0 (or >0) up to the maximum optical power available from the source. While direct modulation of a laser diode appears to match this requirement, operating a laser diode biased at threshold introduces many problems. These include distortion from gain dynamics and high RIN.

In an attempt to overcome this limitation, class B has been explored using FBGs and PM/FM [16]. In principle, input voltage is converted linearly to optical frequency at the transmitter, then a FBG with a reflectivity that is linear with optical frequency is used to provide linear modulated intensity. The resultant filtered optical electric field is square-law detected in a photodetector to produce electrical current. This differs from the standard FM frequency discriminator used in radio systems, in which the input frequency is discriminated to produce voltage (electric field) without the square-law detection. It also differs from normal (class A) optical FM-to-IM conversion using an optical filter (in which the filtered signal is square-law detected), in that the nonlinear threshold in the class-B filter design adds a dramatic complication of both analysis and behavior. This leads to complex interactions between FM conditions, FBG characteristics, and FBG bias conditions.

In this paper, we present a complete theoretical description of this detection/discrimination process and related forms of detection of angle-modulated optical signals. Predictions are confirmed through experimental measurement for a variety of modulation and bias conditions. The paper is organized as follows. In Section II, the requirements for class B in the context of an optical system are described. Expressions are derived for the output of the two FBGs with an FM signal input. In Section III, the experimental setup is described, followed by numerical and experimental results in Section IV, discussion in Section V, and conclusions in Section VI.

II. ANALYSIS

Fig. 1 shows the class B optical link with two FBGs and a balanced detector [16]. We now describe the FM signal and filter characteristics, yielding a general expression for the output of each FBG.

A. Formulation

An angle modulated signal with optical carrier w_c , microwave signal w_m , and modulation index β

$$s(t) = \cos(w_c t + \beta \sin w_m t)$$

= $\sum_{n=-\infty}^{\infty} J_n(\beta) \cos(w_c + nw_m) t.$ (1)



Fig. 2. (a) FBG amplitude response. The FBG power response is linear in the operating range. (b) FM magnitude spectrum at FBG input and output for $\beta = 2$. The frequency in GHz is relative to the optical carrier.

With only a single microwave carrier at a constant w_m , s(t)may be viewed as both an FM and a PM signal, with β interpreted as the phase deviation as well as the frequency deviation divided by w_m . s(t) is converted by the two FBGs FBG1, FBG2 to intensity modulation (IM).

FBG1 may in general be represented as a filter as shown in Fig. 2(a), such that at the discrete frequencies $w_c + nw_m$ present in the spectrum of s(t), the filter output magnitude is $h_n =$ $|H(w_c + nw_m)|$ and with constant group delay τ .

The output of FBG1 is

γ

$$r_{1}(t) = a_{1}(t) \cos[w_{c}t + \phi_{1}(t)]$$

= $\sum_{n=0}^{\infty} h_{n} J_{n}(\beta) \cos[(w_{c} + nw_{m})(t - \tau)]$ (2)

with detected photocurrent (optical power)

$$a_1^2(t) = \left[\sum_{n=0}^{\infty} h_n J_n(\beta) \cos(nw_m t - (w_c + nw_m)\tau)\right]^2 + \left[\sum_{n=0}^{\infty} h_n J_n(\beta) \sin(nw_m t - (w_c + nw_m)\tau)\right]^2$$
(3)

and phase

$$\phi_1(t) = \arctan\left(\frac{\sum_{n=0}^{\infty} h_n J_n(\beta) \sin(nw_m t - (w_c + nw_m)\tau)}{\sum_{n=0}^{\infty} h_n J_n(\beta) \cos(nw_m t - (w_c + nw_m)\tau)}\right).$$
(4)

The output of FBG2 is described by the same expressions with the summation from $-\infty$ to 0 and $h_{-n} = h_n$. To find the spectrum of $a_1^2(t)$, we write $j_n = h_n J_n(\beta)$ for convenience, expand both summations, compute the square of each, add them and simplify using $\cos(u)\cos(v) + \sin(u)\sin(v) = \cos(u-v)$. The result is

$$a_1^2(t) = \sum_{i=-\infty}^{\infty} j_i^2 + 2\sum_{k=1}^{\infty} \sum_{i=-\infty}^{\infty} j_i j_{i+k} \cos(kw_m(t-\tau)).$$
(5)

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As a check, we consider two special cases for the filter h_n . For an all-pass filter $h_n = 1$, $j_n = J_n(\beta)$, there is no discrimination or demodulation, so we expect the envelope $a_1^2(t)$ to be 1. Since $\sum_{-\infty}^{\infty} J_n(z) = 1$, the dc term is 1. Since $J_{-n}(x) =$ $(-1)^n J_n(x)$, all terms at odd multiples of frequencies nw_m are zero. All terms at even multiples are also zero, using the identity [17]

$$0 = \sum_{k=0}^{2n} (-)^k J_k(z) J_{2n-k}(z) + 2 \sum_{k=1}^{\infty} J_k(z) J_{2n+k}(z).$$
(6)

As a second check, if $h_n = K\sqrt{n+n_1}$ so that $j_n = K\sqrt{n+n_1}J_n(\beta)$, where $n_1 \gg 1$ is such that $J_n(\beta) \simeq 0$ for $n > n_1$, and K > 0 is some constant, then we expect class A demodulation. We have numerically verified the envelope $a_1^2(t)$ to be dc plus $\cos[w_m(t-\tau)]$ with negligible higher harmonics (< -100 dB), as expected.

For the FBGs considered here, the amplitude response in Fig. 2(a)

$$H_{1}(w) = 0, w < w_{c}$$

= $g\sqrt{(w - w_{c})}e^{jw\tau}, w_{c} < w < w_{c} + n_{0}w_{m}$
= $e^{jw\tau}, w > w_{c} + n_{0}w_{m}$ (7)

where the constant $g = 1/\sqrt{n_0 w_m}$ is chosen so that the filter gain is 1 at $w = w_c \pm n_0 w_m$ for some n_0 where there are no significant sidebands in s(t). From Carson's rule $n_0 \simeq \beta + 1$. FBG2 is the complementary filter

$$H_{2}(w) = 0, w > w_{c}$$

= $g\sqrt{-(w - w_{c})}e^{jw\tau}, w_{c} - n_{0}w_{m} < w < w_{c}$
= $e^{jw\tau}, w < w_{c} - n_{0}w_{m}.$ (8)

The power responses $|H_1(w)|^2$ and $|H_2(w)|^2$ of the two FBGs are linear in the frequency range of interest. Thus, for FBG1, $h_n = |H(w_c + nw_m)| = \sqrt{n/n_0}$ for $n \ge 0$ and 0 for n < 0, so that $j_n = \sqrt{n/n_0} J_n(\beta)$. However, as a result of imperfections in the filters or by intention, j_0 will in practice be a small nonzero value $j_0 = \sqrt{y/n_0} J_0(\beta)$ with 0 < y < 1.

In this case, $a_1^2(t)$ contains dc and harmonics of all orders

$$a_1^2(t) = \sum_{i=0}^{\infty} j_i^2 + \sum_{k=1}^{\infty} \sum_{i=0}^{\infty} 2j_i j_{i+k} \cos[k(w_m(t-\tau))].$$
(9)

Similarly, for FBG2, $h_n = |H(w_c + nw_m)| = -\sqrt{-n/n_0}$ for $n \le 0$ and 0 for n > 0 and

$$a_2^2(t) = \sum_{i=-\infty}^0 j_i^2 + \sum_{k=1}^\infty \sum_{i=-\infty}^0 2j_i j_{i+k} \cos[kw_m(t-\tau)].$$
(10)

The class B output obtained from the difference $a_1^2(t) - a_2^2(t)$ results in cancelation of the dc and even harmonics, and a doubling of the fundamental and odd harmonics

$$a_1^2(t) - a_2^2(t) = \sum_{k=1,k \text{ odd}}^{\infty} \sum_{i=0}^{\infty} 4j_i j_{i+k} \cos[kw_m(t-\tau)].$$
(11)

The ratio r_k of the kth harmonic to the carrier wave for both a_1^2 and a_2^2 is

$$r_{k} = \frac{\sum_{i=0}^{\infty} j_{i} j_{i+k}}{\sum_{i=0}^{\infty} j_{i} j_{i+1}} = \frac{\sum_{i=0}^{\infty} h_{i} h_{i+k} J_{i}(\beta) J_{i+k}(\beta)}{\sum_{i=0}^{\infty} h_{i} h_{i+1} J_{i}(\beta) J_{i+1}(\beta)}.$$
 (12)

For large β , these results are expected to correspond to those obtained from a half-wave rectified sine wave [17]

$$u(t) = \frac{1}{\pi} + \frac{1}{2} \sin wt - \sum_{k=2,k \text{even}}^{\infty} \frac{2}{\pi} \left(\frac{1}{(k-1)(k+1)} \cos kwt \right)$$
(13)

so that $r_2 = 4/3\pi$, $r_3 = 0$, $r_4 = 4/15\pi$, $r_5 = 0$, and in general $r_k = (4)/(\pi(k-1)(k+1))$ for k even and zero otherwise.

B. Small Modulation Index Analysis

In this subsection, we find the signal relative to dc for small FM index $\beta \ll 1$ using approximations from the series expansion

$$J_n(\beta) = \sum_{l=0}^{\infty} \frac{(-1)^l}{(n+l)!} \left(\frac{\beta}{2}\right)^{2l+n}.$$
 (14)

Fifth-order and higher terms are omitted.

It may be desirable or unavoidable to have some of the carrier leak through the filter, as discussed later. If the leakage at w_c is $h_0 = \sqrt{y/n_0} = \sqrt{x} \neq 0$

$$a_{1}^{2}(t) = [x(1 - \beta^{2}/2) + (\beta^{2}/4 + \beta^{4}/32) + \cos(w_{m}(t - \tau))(x(\beta/2) + \sqrt{2}\beta^{3}/8 + \sqrt{6}\beta^{5}/192) + \cos(2w_{m}(t - \tau))(x\sqrt{2}(\beta^{2}/8) + \sqrt{3}\beta^{4}/48) + \cos(3w_{m}(t - \tau))(x\sqrt{3}(\beta^{3}/48) + \beta^{5}/192) + \cos(4w_{m}(t - \tau))(x\beta^{4}/192 + \beta^{5}/192) + \cos(5w_{m}(t - \tau))(x\sqrt{5}\beta^{5}/3840)]/n_{0}.$$
 (15)

The output of FBG2 is identical, except that the fundamental signal and odd harmonics have the opposite sign.

The class B output is doubled at the odd harmonics and canceled to zero at dc and even harmonics.

III. EXPERIMENTAL SETUP AND APPROACH

Fig. 3 shows the experimental setup to test the theoretical analysis. The output of the external-cavity tunable (ECT) laser is phase modulated by an RF signal at $f_m = w_m/2\pi = 1$ GHz. The phase-modulated optical signal is then amplified using an Erbium-doped fiber amplifier (EDFA) before being directed towards a fiber-Bragg grating (FBG). The specially designed FBG works as an optical frequency discriminator (OFD) with a linear transfer function (power reflectivity versus optical frequency) over 10 GHz, shown as inset in Fig. 3. Thus, $n_0 = 10$, and clipping of significant sidebands will occur for $\beta > 9$.

The FBGs were fabricated by Redfern Optical Components, targeting constant group delay and a linear power reflectivity R over a 10-GHz frequency ramp. Maximum R of each 13-cm-



Fig. 3. Experimental setup. The inset shows the FBG power response.

long grating is 94%. Group delay variations are typically ± 10 ps over the linear portions of the response curve, with larger variations at the corners and over the portions with flat frequency response.

The RF spectra of the reflected light from OFD are measured using a photodetector (O/E) and an electrical spectrum analyzer (ESA), while the waveforms are measured by an optical sampling scope. A practical Class-B link, as reported in [16], consists of two complementary OFD and balanced detection. The link in Fig. 3, with FBG biased at zero, measures effectively the spectral and temporal characteristics of one path of the Class-B link, which is sufficient to validate this analysis.

IV. NUMERICAL AND EXPERIMENTAL RESULTS

Numerical results are shown in both time and frequency domains, followed by experimental results.

Figs. 4–6 show $a_1^2(t)$, $a_2^2(t)$ and $a_1^2(t) - a_2^2(t)$ for different values of β with x = 0. We observe that for $\beta = 0.5$, each FBG output contains a significant dc component (which cancels in class B), and low harmonic distortion. For $\beta = 2.0$ the dc component from each FBG is smaller relative to the signal component, but the odd harmonic distortion is increased. For $\beta = 8.0$, the dc component of each FBG output approaches its smallest possible value (half of the peak to peak signal component), but the harmonic distortion in each FBG output is quite apparent. For the latter case, the FBG outputs begin to approximate the expected ideal class B operation. For $\beta > 20$ (not shown), the complementary signals appear as half-wave rectified cosine waves, and the output approximates a cosine wave. These results can also be observed using a frequency domain view of the FBG outputs. For the class B output of the balanced detector, the signal and odd harmonics are doubled, and the dc and even harmonics are canceled out.

Values of the dc component, desired signal component (fundamental) and harmonics of $a_1^2(t)$ are plotted versus β in Fig. 7 using (9) with carrier leakage x = 0 and for β up to 0.5, showing that the signal curve 1 increases with β^3 . Fig. 8 shows the corresponding values with x = 0.1. In this case, the signal curve 1 increases linearly with β (from the signal term in (15), the linear term dominates when $\beta^2 > 4x/\sqrt{2}$). Operating with some residual carrier leads to a linear input-output relationship with significant dc, typical of class A links.

Fig. 9 shows values of the dc component, desired signal component (fundamental) and harmonics of $a_1^2(t)$ versus β over a larger range of β up to 2.5 and harmonics up to the 5th, with



Fig. 4. Class B waveforms, $\beta = 0.5$.



Fig. 5. Class B waveforms, $\beta = 2$.



Fig. 6. Class B waveforms, $\beta = 8$.

x = 0. For large β , the absolute value of power in the odd harmonics increases linearly with β .

Fig. 10 shows the ratio of the kth harmonic to dc, and Figs. 11 and 12 show the ratio of the kth harmonic to carrier for k = 2, 3, 4, and 5 with x = 0. Fig. 12 is a magnified view of Fig. 11. The ratios increase with β for small β to reach a peak value for β in the range 3 to 4. For large $\beta > 10$, the ratios approach a



Fig. 7. Detected voltage harmonics versus β at one FBG output.



Fig. 8. Detected voltage harmonics versus β at one FBG output with carrier leakage.



Fig. 9. Optical power (detected voltage) harmonics versus β at one FBG output.

constant value near the ratios expected for a half-wave rectified cosine wave.



Fig. 10. Ratio of harmonics to dc versus β at one FBG output.



Fig. 11. Ratio of harmonics to signal voltage versus β at one FBG output.

In particular, Fig. 10 shows the signal-to-dc ratio is as high as it can be for a rectified cosine wave signal. Figs. 11 and 12 show that the third-order harmonic distortion at one FBG output is low for small β , maximum for intermediate β , and reduces towards zero as β is further increased. Thus, for large β the FBG filter shape in (7) simultaneously achieves both the lowest possible dc (i.e., the dc component of a rectified cosine wave) and low third-order harmonic distortion at each FBG output (which leads to maximum SDFR in class B operation [15]). However, this ideal class B result is obtained only for β greater than about 20.

To confirm these theoretical results, Figs. 13–16 show the power of one FBG output from (5) for specified values of β and x, along with the corresponding measured results in both time and frequency domains. Fig. 13 shows one cycle of the detected voltage for $\beta = 0.5$, x = 0.05. Aside from a slight phase shift, agreement between theory and experiment is reasonable. Fig. 14 shows the power spectrum of the detected voltage at one FBG output, obtained by taking the fast Fourier transform (FFT) of the five cycles of the time domain waveform that were recorded. The agreement between theory and FFT is excellent; however, the actual frequency domain measurements agree less well but



Fig. 12. Ratio of harmonics to signal voltage versus β at one FBG output, magnified view of previous figure.



Fig. 13. Detected voltage at one FBG output, $\beta = 0.5$, x = 0.05.

still reasonably. Fig. 15 shows one cycle of the detected voltage for $\beta = 2.0, x = 0.05$, and Fig. 16 shows the frequency domain results. Agreement between theory and experiment is similar to that for Figs. 13 and 14. Measurements for $\beta = 8$ could not be obtained due to limitations on the RF power, and thus FM clipping was not a factor in the experiments.

The full class B system with two FBGs was not implemented. The single FBG results reported here are of value regardless, since they confirm the analysis showing that ideal class B FM can be achieved with a large modulation index.

V. DISCUSSION

Equation (15) shows that for small β , class B operation results in third-order distortion that is fundamental to the detection process and must be considered in link performance. The ratio of third-order (third harmonic) distortion to signal (3HD/S), given by (15) and assuming sufficient carrier leakage that the x terms dominate, is $\beta^2/13.7 = m^2/3.43$, where the modulation index (signal/dc) $m = \beta/2$. For a quadrature-biased MZ modulator, $3HD/S = m^2/24$. Therefore, third-order distortion for small β is substantially worse than an MZ intensity modulator.



Fig. 14. Power spectrum of detected voltage at one FBG output, $\beta=0.5, x=0.05.$



Fig. 15. Detected voltage at one FBG output, $\beta = 2.0, x = 0.05$.



Fig. 16. Power spectrum of detected voltage at one FBG output, $\beta=2.0, x=0.05.$

In contrast, for large β , class B operation results in the ratio of third-order distortion to signal reducing towards zero as β is increased, and the signal/dc ratio is the $\pi/2$ value for a half-wave



Fig. 17. Optimum class B filter amplitude response for $\beta = 8$. The frequency in GHz is relative to the optical carrier.

rectified cosine wave. Shot noise and RIN are functions of dc and thus are substantially lower for ideal class B operation with large β than for conventional links [15].

The essential result is that class B FM does achieve low dc and low third-order harmonic distortion, but only for large β . This may appear counter-intuitive, since for all values of β including small β , the instantaneous frequency varies sinusoidally above and below w_c and thus the FBG output might be expected to be a rectified cosine wave with low dc and low third-order harmonic distortion. However, the results show that for small β this is not the case. The reason this intuition fails is that combining a time-domain view of the FM signal (instantaneous frequency, not averaged over time) with a frequency domain view of the FBG filter response is inconsistent with the frequency domain analysis in (2).

In the Appendix, we find an "optimum" filter shape that does achieve both low dc and low third-order distortion simultaneously for any β including small β , but this filter shape depends on β and thus is not practical to implement over a range of β .

VI. CONCLUSION

A class-B MPL using optical FM and fiber-Bragg gratings is analyzed and results verified with measurements. Input voltage is converted linearly to FM, and this FM is converted by each FBG to intensity modulation (IM). The balanced detector subtracts currents generated in each detector, yielding an effective transfer function with zero dc. The signal increases as β^3 for small β , becoming linear in β with carrier leakage. This carrier leakage makes the class B link behave more like a suppressed carrier class A link, and may generally provide adequate reduction in dc-related noise. We have quantified the level of third-order distortion that results from the sideband filtering operation, and shown that for small β , this is worse than for a MZ intensity modulator. However, for large β , class B operation operates as expected, simultaneously achieving low dc and low third-order distortion, and thus substantially reduces IM3, shot noise, and RIN, as reported in [15]. Ideal class B operation can be realized for large index FM modulation only.

APPENDIX

In this Appendix, we consider a more optimum filter shape h_n which achieves both low dc and low third-order harmonic distortion for both large and small β . The desired filter output will have an envelope appearing as a rectified cos wave $s_{\text{rectcosFM}}(t) = s_{\text{rectcos}}(t) \cdot s_{\text{FM}}(t)$. An FM signal with an exact rectified cosine envelope has a spectrum $S_{\text{rectcosFM}}(f) = S_{\text{rectcos}}(f) \otimes S_{\text{FM}}(f)$. The ratio $H_{\text{opt}}(f) = S_{\text{rectcosFM}}(f)$ is the transfer function of a filter which yields $s_{\text{rectcosFM}}(t)$ in response to input $s_{\text{FM}}(t)$. Note that H_{opt} has a nonzero response on both sides of the carrier, and is optimum for only one particular value of β . For large $\beta = 8$ (Fig. 17), the optimum filter begins to approximate the FBG transfer function (7) shown in Fig. 2(a).

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