

# ELEC 621

## Numerical Techniques in Electromagnetics

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Lecture 1 General Info and Theoretical Foundations

Wolfgang J.R. Hoefer



Computational Electromagnetics  
Research Laboratory  
University of Victoria, Canada



## Objectives

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1. Meet the students, get their names and addresses, discuss modalities, assessment, etc.
2. Introduce course philosophy and content. Show course webpage. Give references.
3. Explain significance of electromagnetic modeling in modern CAD design. Stress the importance of modeling both in frequency and time domains.
4. Compare traditional and alternative approaches to modeling. Discuss challenges and limitations.
5. Introduce students to the general methodology for field analysis, the classification, and the general features common to all field modeling methods.
6. Discuss frequency domain vs. time domain concepts.



## Lecture Structure

- I. Introduction, motivation and historical perspective
  1. Importance of numerical modeling.
  2. Driving forces in field modeling.
  3. Why computers are needed in modern electromagnetic design. Understanding CAD.
  4. Functions performed by CAD programs. Traditional and alternative solution of electromagnetic problems.
  5. Methods for solving electromagnetic problems.
  6. Classification of methods and their general properties.
  7. Frequency vs. time domain concepts.

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Lecture 1 - 2



## Access to the Course page

<http://www.ece.uvic.ca/~whoefler>




All documents for distribution to the class will be posted on the course page. Check periodically.

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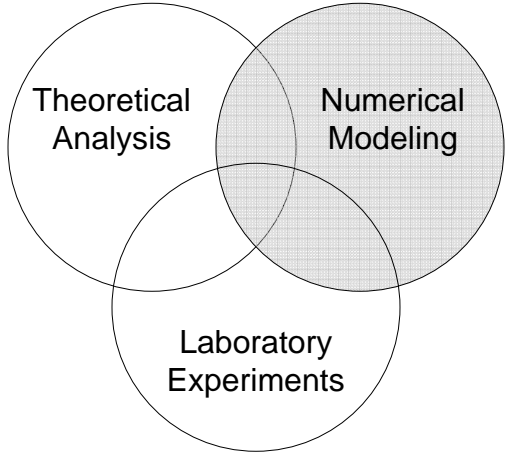
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## Introduction

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**The Three Pillars of Electromagnetic Microwave and Lightwave Engineering**

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## Importance of Numerical Modeling

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- Key to analysis, design and optimization of r.f. to optical systems.
- Basis for field-theory based and process-oriented CAD.
- Key to economical success of a product through shortening of development time.
- Only means for dealing with complex electromagnetic structures.
- Suitable for creating CAD tools and expert systems.
- Theoretical models must be validated by experiments. Theoretical and experimental work are of equal importance.


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## What Drives Field Modeling ?

Driving Forces in Field Modeling	Examples
<p><b>Hardware Availability:</b></p> <ul style="list-style-type: none"> <li>• Computers with large memory and clock rates</li> <li>• Vector and parallel processors</li> </ul> <p><b>Structures and processes to be modeled:</b></p> <ul style="list-style-type: none"> <li>• Circuits of high complexity and density</li> <li>• Impulsive waveforms and transients</li> <li>• Nonlinear and time effects</li> <li>• EMI/EMC and crosstalk effects</li> <li>• Packaging effects and signal integrity</li> </ul> <p><b>Requirements of Designers and Users:</b></p> <ul style="list-style-type: none"> <li>• User-friendly interface with modeling tool</li> <li>• Flexibility and versatility of modeling tool</li> <li>• Field visualization and animation</li> <li>• Engineering parameter extraction</li> </ul>	<p>Workstations, Supercomputers Parallel Processors</p> <p>Monolithic circuits, interconnects High speed digital/mixed signal circuits Solid state devices, superconductors High speed logic and communication MW and mmW Integrated Circuits</p> <p>Geometry and process-oriented tools EM Simulators, multi-level simulation Dynamic 3D graphics, color maps S-parameters from field solutions</p>

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## Classic Electromagnetic Solution

*Mathematical Formulation*

*Analytical Preprocessing*

*Discretization*

*Postprocessing*

Maxwell's Equations

Boundary Conditions

Material Properties

Analytical Model

←

Problem-dependent

Computer Program

↓

User Data

Computation

↓

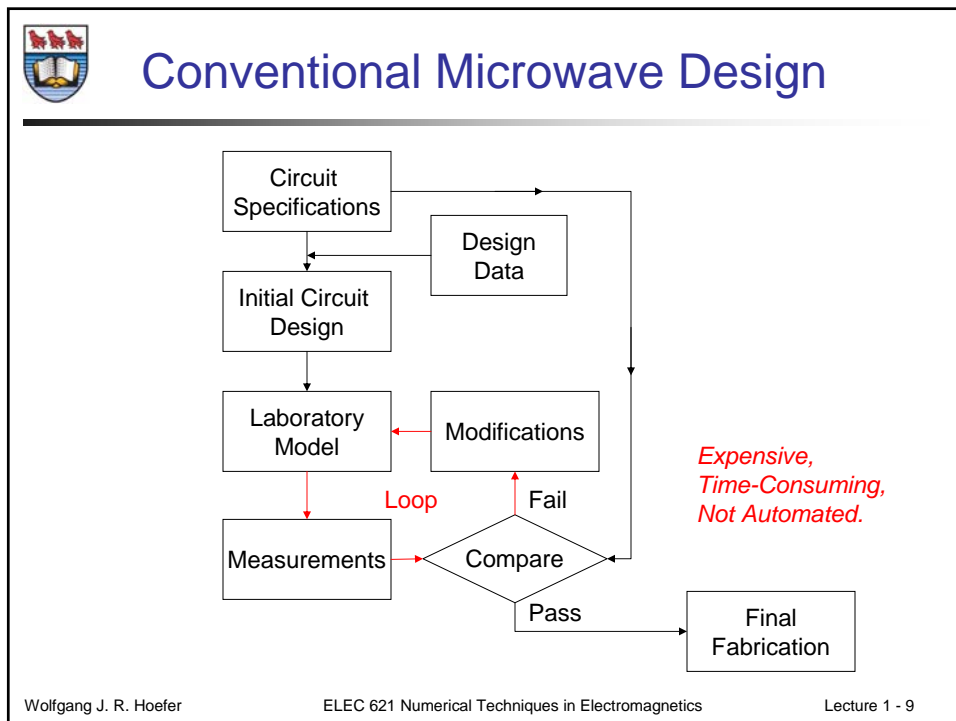
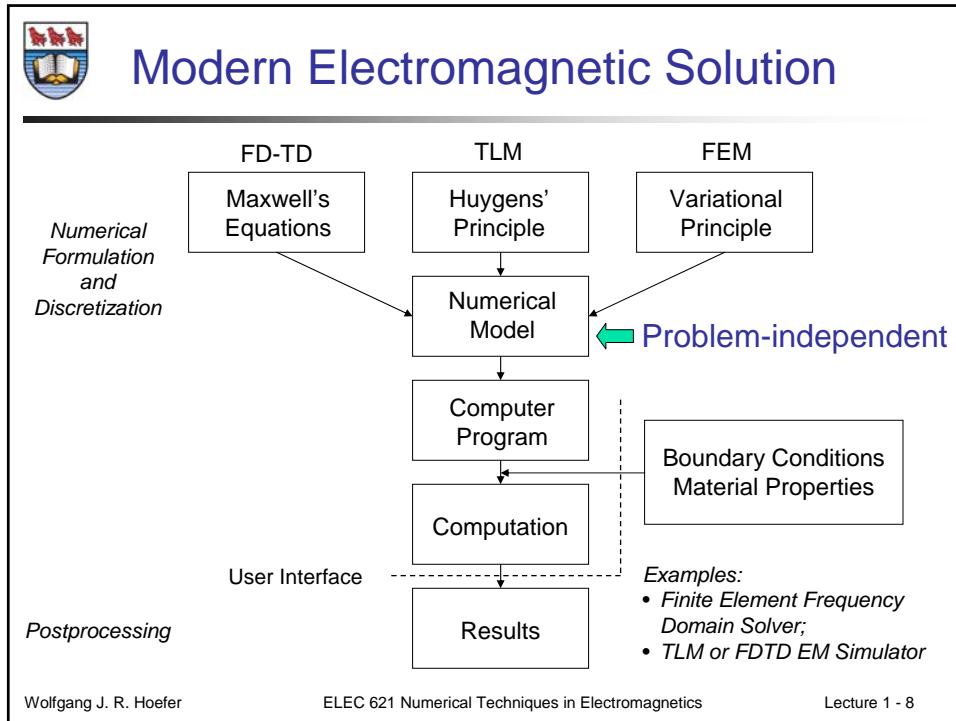
Results

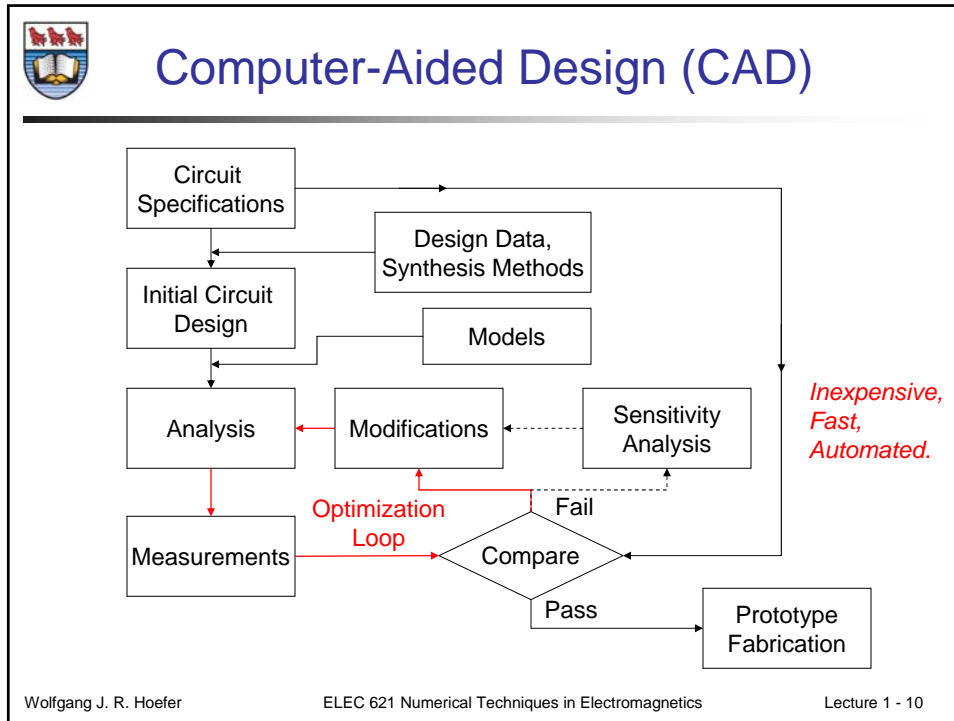
User Interface

*Examples:*

- Closed-form expressions for microstrip;
- spectral domain program for coplanar waveguides;
- mode-matching program for waveguide filters;

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- CAD Functions**
- Planning
  - Synthesis
  - Partitioning
  - Modeling
  - Simulation
  - Layout
  - Verification
  - Testing
  - Documentation
  - Inventory
  - Etc...
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## Electromagnetic Simulators

- An Electromagnetic Simulator is a field modeling tool that
  - solves electromagnetic field problems by numerical analysis;
  - extracts engineering parameters from the field solution and visualize fields and parameters;
  - allows design by means of analysis combined with optimization.
- The field solver engine employs one or several numerical methods obtained through the practice of Numerical Electromagnetics.

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## Numerical Electromagnetics (NE)

- Numerical Electromagnetics is the theory and practice of solving electromagnetic field problems on digital computers;
- It provides the only viable approach to solving "real world" field problems;
- It enables Computer-Aided Engineering (CAE) and Computer-Aided Design (CAD) of electromagnetic components and systems.

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## Models of Light Propagation 1

- **Pythagoras**                      **6th century B.C.**  
*Light is a stream of particles emitted from a source of light.*
- **Demokritos**                      **460-370 B.C.**  
*All objects consist of a large number of particles: the atoms. Images are transmitted by atoms detaching themselves from the surface of objects and drifting through space.*
- **Aristotle**                              **384-322 B.C.**  
*Light moves as a wave, like ripples on the water.*
- **Newton**                                **1662-1727**  
*Light is made up of tiny particles (corpuscles) that fly through space.*

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## Models of Light Propagation 2

- **Huygens**                              **1629-1695**  
*Light is transmitted in the form of shock waves made up by the superposition and succession of elementary spherical disturbances of the Ether (Huygens' Principle).*
- **Maxwell**                                **1831-1879**  
*Light is an electromagnetic wave governed by the interaction of electric and magnetic fields (Maxwell's Theory, experimentally confirmed by Hertz).*
- **Einstein/de Broglie**              **20th Century**  
*Light has both particle and wave properties. These aspects are complementary. One or the other dominates, depending on the phenomenon under study.*

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## Solving EM Field Problems

- Find electromagnetic field and/or source functions such that they
  - obey Maxwell's equations,
  - satisfy all boundary conditions,
  - satisfy all interface and material conditions,
  - satisfy all excitation conditions.

(in both time and space, or at one freq. in space)
- The solution is generally unique (Analysis)

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## Field-Solving Methods


Methods for solving Maxwell's Equations:

- Analytical Methods
  - Exact explicit solutions (only a few ideal cases)
- Semi-Analytical Methods
  - Explicit solutions requiring final numerical evaluation
- Numerical Methods
  - Differential or integral equations are transformed into matrix equations by projective approximations and solved iteratively or by matrix inversion

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## Classification of Methods 1

Frequency Domain Methods  
(Time-Harmonic)

Time Domain Methods  
(Transient)


Fourier Transform

*This distinction is based more on human experience than on physical or mathematical considerations.*

*The time dimension can be treated as a fourth dimension in Minkowski space in the form  $jct$ , where  $c$  is the speed of light.*

In the most general sense, solution methods can thus be classified according to the number of dimensions upon which the field and source functions depend.

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## Classification of Methods 2

- 1D Methods: Fields and voltage/current vary in **one** space dimension (Transmission Line Problems)  
(...Touchstone, Supercompact, SPICE....)
- 2D Methods: Fields and currents vary in **two** space dimensions (Cross-section problems,  $TE_{n0}$  waveguide problems)  
(...FEM-2D, MEFiSTo-2D....)
- 2 1/2 D Methods: Fields vary in **three** space dimensions, currents vary in **two** space dimensions (Planar multilayer circuits)  
(...Sonnet, Momentum, Ensemble ....) frequency domain
- 3D Methods: Fields and currents vary in **three** space dimensions (General propagation, scattering and radiation problems)  
(...HFSS, FEFS, MEFiSTo-3D, CST, Quickwave..)

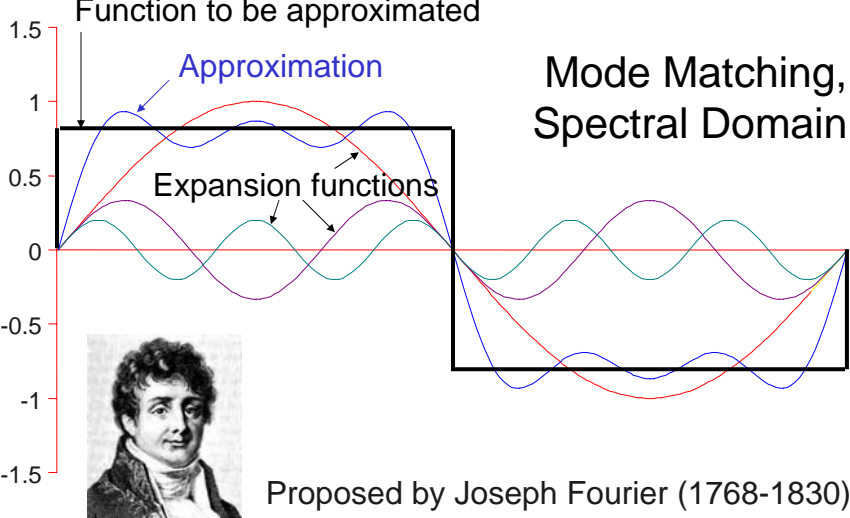
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## Full-Domain Expansion Functions


Function to be approximated



Approximation


Expansion functions

Mode Matching,  
Spectral Domain



Proposed by Joseph Fourier (1768-1830)

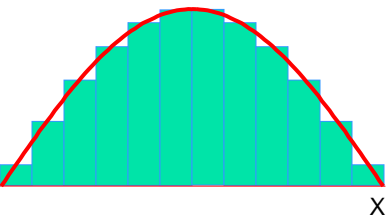
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## Subsectional Expansion Functions

$F(x)$

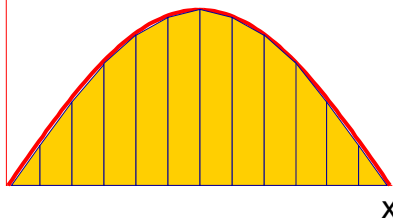
Finite Differences



X

$F(x)$

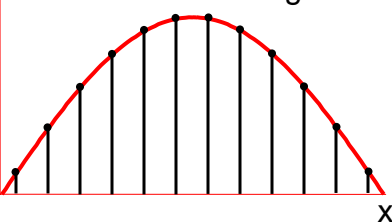
Finite Elements



X

$F(x)$

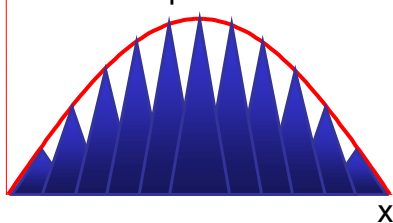
Point Matching



X

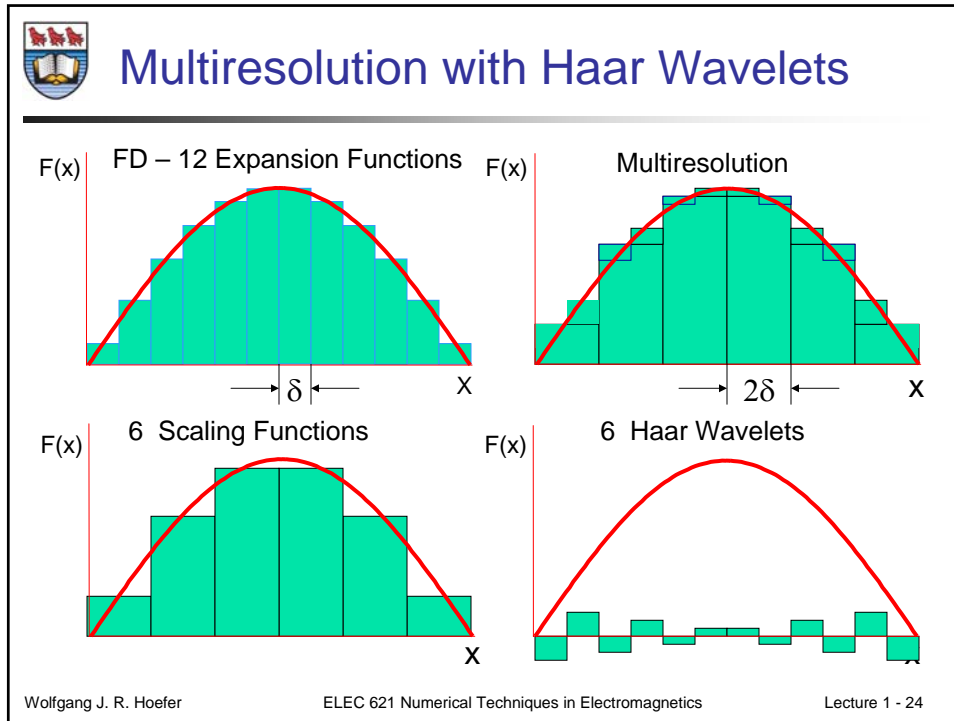
$F(x)$

Rooftop Functions



X

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- The diagram is titled "Frequency and Time Domain Concepts" and lists various concepts in two columns:
- Complex Frequency
  - Phase angle
  - Complex Dielectric Constant
  - Complex Reflection/Transmission Coeff.
  - Complex Impedance
  - Q-Factor
  - Complex multiplication
  - Time dependence
  - Delay
  - Real permittivity and conductivity
  - Reflection/Transmission time response
  - Impulse response
  - Decay time
  - Time domain convolution
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## Why model in the frequency domain?

- Most microwave engineers are more familiar with FD concepts than with TD concepts,
- Frequency domain simulations are steady-state,
- Complex notation is elegant and efficient,
- Specifications are traditionally formulated in the FD (S-Parameters, loss tangent, dispersion),
- Time domain information can be obtained by inverse Fourier Transform (Causality issues!),
- Dispersive materials and boundaries are easily described by frequency-dependent parameters.

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## Why model in the time domain?

- Time domain simulations are life-like
- Virtual experiments are set up as in the lab (Source, reference planes, output probes)
- Cause and effect can be distinguished
- One simulation can cover a wide bandwidth
- Transient phenomena can be simulated
- Nonlinear behavior is modeled naturally
- Dispersive materials and boundaries are modeled in a more physical manner

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## Summary and Conclusions

- Numerical Methods allow us to solve real life electromagnetic problems. They form the engine of electromagnetic simulators.
- Electromagnetic simulators are not merely Maxwell equation solvers, but powerful simulation and design tools with visualization capabilities.
- Understanding the underlying numerical methods is essential in assessing the accuracy, performance and limitations of a particular simulation tool.
- Electromagnetic simulators are the heart of modern CAD tools for analog microwave, digital high-speed and mixed signal design, EMC and signal integrity engineering and other applications of electromagnetic fields and waves.